

Students are to answer **30 questions**. The breakdown is as shown below.

Time allowed **1h: 30mins**

Section 1----- 3 questions

Section 2----- 3 questions

Section 3----- 2 questions

Section 4----- 2 questions

Section 5----- 2 questions

Section 6----- 2 questions

Section 7----- 2 questions

Section 8----- 2 questions

Section 9----- 2 questions

Section 10----- 2 questions

Section 11----- 1 question

Section 12----- 1 question

Section 13----- 1 question

Section 14----- 2 questions

Section 15----- 1 question

Section 16----- 1 question

Section 17----- 1 question

# SECTION 1

^^ When two conjoined cones at the apex are dissected vertically parallel to the vertical height, the resulting cross-sectional shape is that of a/an

@@ Ellipse

@@ Circle

@@ Parabola

@@ Hyperbola ~

^^ When a cone is dissected parallel to the slanting side, the resulting cross-sectional shape is that of a/an

@@ Ellipse

@@ Circle

@@ Parabola ~

@@ Hyperbola

^^ When a cone is dissected at an orientation that is neither parallel to the slanting side nor the circular base, the resulting cross-sectional shape is that of a/an

@@ Ellipse ~

@@ Circle

@@ Parabola

@@ Hyperbola

^^ When a cone is dissected parallel to the circular base, the resulting cross-sectional shape is that of

@@ Ellipse

@@ Circle ~

@@ Parabola

@@ Hyperbola

^^ The coordinate of the focus of the curve represented by  $y = 3t + 1$  and  $x = t^2 - 2$  is

@@  $\left(\frac{1}{4}, 1\right)$  ~

@@  $\left(\frac{13}{4}, 1\right)$

@@  $\left(\frac{5}{4}, -1\right)$

@@  $\left(-\frac{13}{4}, -1\right)$

^^ The coordinate of the focus of the curve represented by  $y = 4t + 1$  and  $x = t^2 - 2$  is

@@  $(2, 1)$  ~

@@  $(4, 1)$

@@  $(-2, -1)$

@@  $(4, -1)$

^^ The focus of the Parabola  $(y - 1)^2 = 8(x - 2)$  is located at

@@  $(4, 1)$  ~

@@  $(2, 1)$

@@  $(1, 2)$

@@  $(1, 4)$

^^ \_\_\_\_\_ is the set of all points that satisfy a set of condition

@@ Directrix

@@ Focus

@@ Locus ~

@@ Vertex

^^ The parabola whose vertex is at (2, 1) and focus 2 units way from the vertex having its axis of symmetry parallel to the X-axis is

@@  $(y - 1)^2 = 12(x - 2)$

@@  $(x + 2)^2 = 8(y + 1)$

@@  $(x - 2)^2 = 12(y - 1)$

@@  $(y - 1)^2 = 8(x - 2)$  ~

^^ At both ends of the Latus Rectum to the Parabola  $y^2 = 4ax$ , tangents are drawn. The two tangents meet

@@ on the directrix ~

@@ at the vertex

@@ at the focus

@@ on the normal

^^ The Parabola  $y^2 - 2y = 4x + 3$  has its focus at

@@ (-1, -1)

@@ (1, 1)

@@ (-1, 1)

@@ (0, 1) ~

^^ An ellipse with center at the origin has eccentricity  $\frac{1}{2}$ . If the distance between both

vertices is 8, what is the distance between a focus and its corresponding directrix?

@@ 8

@@ 6 ~

@@ 4

@@ 5

^^ One focus of the ellipse  $\frac{x^2}{16} + \frac{y^2}{4} = 1$  is at

@@  $(2\sqrt{3}, -2\sqrt{3})$

@@  $(2\sqrt{3}, 0)$  ~

@@  $(0, -2\sqrt{3})$

@@  $(0, -2\sqrt{3})$

^^ If the ellipse  $\frac{x^2}{16} + \frac{y^2}{4} = 1$  has a focus at S and the corresponding vertex at Q. What is the coordinates of P; the mid-point of the line segment SQ

@@  $(3 + \sqrt{2}, 0)$

@@  $(3\sqrt{2}, 0)$

@@  $(2 + \sqrt{3}, 0)$  ~

@@  $(2\sqrt{3}, 0)$

^^ A parabola is the only conic that has

@@ a unity eccentricity ~

@@ focus

@@ vertex

@@ line of symmetry

^^ The center of a hyperbola is at the origin and one vertex is at  $(4,0)$ . If the line  $x = 2$  is a directrix, what is the coordinates of a focus of the hyperbola

@@  $(4, 0)$

@@  $(2, 0)$

@@  $(4, 2)$

@@  $(8, 0)$  ~

^^ The center of a hyperbola is at the origin and one vertex is at  $(4,0)$ . If the line  $x = 2$  is a directrix, what is the distance between a focus and its associated vertex?

@@ 4 ~

@@ 8

@@ 6

@@ 2

^^ A hyperbola with center at  $(1, 1)$  and eccentricity  $e = \frac{3}{2}$  has a focus at  $(10, 1)$ . The coordinates of a vertex is?

@@  $(1, 7)$

@@  $(1, 6)$

@@  $(7, 1)$  ~

@@  $(6, 1)$

^^ The following is/are true of rectangular hyperbolas with center at the origin

I  $e^2 - 2 = 0$     II  $e = \sqrt{2}$     III vertex at  $(a, a)$     IV focus at  $(ae, 0)$

@@ I and IV only

@@ II, III and IV only

@@ All of the above

@@ I, II and IV only ~

^^ An ellipse with center at the origin has eccentricity  $\frac{1}{2}$ . If the distance between both vertices is 8, what is the distance between the two foci?

@@ 8

@@ 6

@@ 2

@@ 4 ~

^^ An ellipse has its foci at  $(6,0)$  and  $(-6,0)$ . If the length of its major axis is 14, the length of the minor axis is

@@  $2\sqrt{13}$  ~

@@  $3\sqrt{13}$

@@  $13\sqrt{2}$

@@  $2\sqrt{5}$

^^ An ellipse has its foci at  $(6,0)$  and  $(-6,0)$ . If the length of its major axis is 14, find its

equation

@@  $\frac{x^2}{7} + \frac{y^2}{13} = 1$

@@  $\frac{x^2}{49} + \frac{y^2}{13} = 1$  ~

@@  $\frac{x^2}{13} + \frac{y^2}{49} = 1$

@@  $\frac{x^2}{14} + \frac{y^2}{13} = 1$

^^ An ellipse has its foci at (6,0) and (-6,0). If the length of its major axis is 14, the value of its eccentricity is

@@  $\frac{3}{4}$

@@  $\frac{5}{6}$

@@  $\frac{3}{5}$

@@  $\frac{6}{7}$  ~

^^ A given hyperbola has its center at the origin and one vertex at (4,0). If the line  $x = 2$  is the corresponding directrix, what is the distance between the foci?

@@ 8

@@ 16 ~

@@ 10

@@ 12

^^ A given hyperbola has its center at the origin and one vertex at (4,0). what is the distance between the vertexes?

@@ 8 ~

@@ 16

@@ 10

@@ 12

## SECTION 2

^^ The eccentricity ( $e$ ) of the ellipse  $2(x^2 + 2y^2) - 8y + 8x = -4$  is

@@  $\sqrt{\frac{1}{2}}$  ~

@@  $\frac{1}{2}$

@@ 1

@@ 4

^^ If the length of the major axis and the eccentricity of an ellipse are 10 and  $\frac{3}{5}$  respectively, find the length of the semi-minor axis

@@ 8

@@ 4 ~

@@ 16

@@ 2

^^ An ellipse with center at the origin has eccentricity  $\frac{1}{2}$ . If the distance between both vertices is 8, what is the length of Latus Rectum?

@@  $2\sqrt{3}$

@@ 5

@@ 4

@@ 6 ~

^^  $y^2 = 8x$  and  $y^2 = 32x$  are equations of two Parabolas with eccentricities  $e_1$  and  $e_2$  respectively. Which of the followings is/are true:

I  $e_1 > e_2$

II  $e_1 < e_2$

III  $e_1 - e_2 = 0$

IV  $e_1 + e_2 = 2$

@@ I only

@@ III and IV ~

@@ II only

@@ I and IV

^^ The range of eccentricity of the hyperbola is \_\_\_\_\_

@@  $1 < e < \infty$  ~

@@  $0 < e < 1$

@@  $0 < e < \infty$

@@  $\sqrt{2} < e < \infty$

^^ A conic with eccentricity  $e = \sqrt{6}$  must be a/an \_\_\_\_\_

@@ Parabola

@@ Ellipse

@@ Rectangular hyperbola

@@ Hyperbola ~

^^ Which of the following is a true property of an eccentricity ( $e$ )

@@  $-\infty < e < 0$

@@  $0 \leq e \leq \infty$  ~

@@  $e = \sqrt{-1}$

@@ e = -1

^^ The eccentricity of a conic section is  $\frac{1}{2}$ , if the length of its major axis is 8, what is the length of its semi-minor axis

@@  $3\sqrt{2}$

@@  $4\sqrt{5}$

@@  $2\sqrt{3}$  ~

@@ 6

^^ An ellipse with center at the origin has eccentricity  $\frac{1}{2}$ . If the distance between both vertices is 8, what is the distance between the two directrices?

@@ 16 ~

@@ 14

@@ 12

@@ 10

^^ The semi Major axis and eccentricities of two ellipses are:  $E_1(a = 4, e = \frac{1}{2})$  and

$E_2(a = 3, e = \frac{2}{3})$ . If they both share a common center at the origin, the distance between their foci is

@@ 1

@@  $\frac{1}{2}$

@@  $\frac{2}{3}$

@@  $\frac{2}{3}$

@@ 0 ~

@@ 0 ~

^^ The eccentricity of the curve represented by the equations  $x + 1 = 5\cos\theta$  and  $y - 2 = 4\sin\theta$  is

@@  $\frac{3}{5}$  ~

@@  $\frac{\sqrt{5}}{3}$

@@  $\frac{4}{9}$

@@  $\frac{9}{5}$

^^ The semi-Major axis and eccentricities of two ellipses are:  $E_1(a = 4, e = \frac{1}{2})$  and

$E_2(a = 3, e = \frac{1}{3})$ . If they both share a common center at the origin, the distance between their directrices is

@@ 1 ~

- @@ 3
- @@ 4
- @@ 4.5

^^ The semi Major axis and eccentricities of two ellipses are:  $E_1(a = 4, e = \frac{1}{2})$  and  $E_2(a = 3, e = \frac{2}{3})$ . If they both share a common center at the origin, the absolute difference between their Major axes is

- @@ 5
- @@ 3
- @@ 4
- @@ 2 ~

^^ Let  $x^2 + 4y^2 - 2x + 4y - 2 = 0$  be the equation of an ellipse. The value of the eccentricity of this ellipse is

- @@  $\frac{3}{5}$
- @@  $\frac{2}{3}$
- @@  $\frac{4}{5}$  ~
- @@  $\frac{2}{5}$

^^ The center of a hyperbola is at the origin and one vertex is at  $(4,0)$ . If the line  $x = 2$  is a directrix, what is the value of its eccentricity?

- @@ 4
- @@ 2 ~
- @@  $\frac{1}{2}$
- @@  $\frac{3}{2}$

^^ The eccentricity of a conic can be any of the following except

- @@ -1 ~
- @@ 0
- @@  $\sqrt{2}$
- @@ 0.5

^^ The eccentricity of the curve represented by the equations  $x = 3\cos\beta$  and  $y = 2\sin\beta$  is

- @@  $\frac{\sqrt{3}}{5}$
- @@  $\frac{\sqrt{5}}{3}$  ~
- @@  $\frac{4}{9}$
- @@  $\frac{9}{5}$

^^ The conic whose eccentricity is  $\sqrt{2}$  must be a/an

@@ parabola

@@ ellipse

@@ rectangular hyperbola

@@ hyperbola ~

^^ The eccentricity of a rectangular hyperbola is

@@  $\sqrt{3}$

@@  $\sqrt{2}$  ~

@@  $\sqrt{5}$

@@  $\sqrt{7}$

## SECTION 3

^^ The equation of normal to the parabola  $3x^2 + 6x - 12y = 0$  at  $P(2, 2)$  is \_\_\_\_\_

@@  $2y - 3x + 2 = 0$

@@  $2y + 3x - 10 = 0$

@@  $3y + 2x - 10 = 0$  ~

@@  $3y - 2x - 2 = 0$

^^ The equation of normal to the parabola  $3x^2 + 6x - 12y = 0$  at  $P(0, 1)$  is \_\_\_\_\_

@@  $y + 2x - 1 = 0$  ~

@@  $2y + 3x - 10 = 0$

@@  $3y + 2x - 10 = 0$

@@  $3y - 2x - 2 = 0$

^^ The equation of normal to the parabola  $3x^2 + 6x - 12y = 0$  at  $P(0, -1)$  is

@@  $y + 2x + 1 = 0$  ~

@@  $2y + 3x - 10 = 0$

@@  $3y + 2x - 10 = 0$

@@  $3y - 2x - 2 = 0$

^^ The equation of normal to the parabola  $3x^2 + 6x - 12y = 0$  at  $P(0, -2)$  is

@@  $y + 2x - 2 = 0$  ~

@@  $2y + 3x - 10 = 0$

@@  $3y + 2x - 10 = 0$

@@  $3y - 2x - 2 = 0$

^^ The equation of Normal to the Parabola  $x^2 - 6x - 8y + 1 = 0$  at the point  $(1, \frac{1}{2})$  is

@@  $2x + 4y + 5 = 0$

@@  $2x + y - 5 = 0$

@@  $2y - 4x + 5 = 0$  ~

@@  $2y - x - 5 = 0$

^^ The equation of Normal to the Parabola  $x^2 - 6x - 8y + 1 = 0$  at the point  $(1, 0)$  is

@@  $2x + 4y + 5 = 0$

@@  $2x + y - 5 = 0$

@@  $y - 2x + 2 = 0 \sim$

@@  $2y - x - 5 = 0$

^^ The equation of Normal to the Parabola  $x^2 - 6x - 8y + 1 = 0$  at the point (1, -1) is

@@  $2x + 4y + 5 = 0$

@@  $2x + y - 5 = 0$

@@  $y - 2x + 3 = 0 \sim$

@@  $2y - x - 5 = 0$

^^ The equation of a normal to the parabola  $y^2 = 4x$  at (0, 1) is given by

@@  $y - 2x = -1$

@@  $y + 2x = 1$

@@  $2y + x + 1 = 0$

@@  $2y - x = 2 \sim$

^^ The equation of a normal to the parabola  $y^2 = 4x$  at (1, 1) is given by

@@  $y - 2x = -1$

@@  $y + 2x = 1$

@@  $2y - 2x + 1 = 0$

@@  $y - 2x = -1 \sim$

^^ The slope of the normal at any point on the rectangular hyperbola  $x = ct, y = ct^{-1}$  is

@@  $ct$

@@  $-t^{-2}$

@@  $t^2 \sim$

@@  $-ct$

^^ The equation of normal to the ellipse  $x^2 + 5y^2 = 25$  at the point (1,2) is

@@  $y = x - 1$

@@  $y = 5x - 2$

@@  $y = 5x + 3$

@@  $y = 5x - 3 \sim$

^^ The equation of normal to the curve  $x^2 = 6y$  at the point (2, 1) is

@@  $2y + 3x - 8 = 0 \sim$

@@  $2y + 3x + 8 = 0$

@@  $3y + 2x - 8 = 0$

@@  $2y - 3x - 8 = 0$

^^ The equation of normal to the curve  $x^2 = 6y$  at the point (3, 1) is

@@  $2y + x - 5 = 0 \sim$

@@  $2y + 3x + 5 = 0$

@@  $3y + 2x - 8 = 0$

@@  $2y - 3x - 8 = 0$

^^ The condition for the line  $y = mx + k$  to be a tangent to the conics  $b^2x^2 - a^2y^2 = a^2b^2$  is

@@  $k = \pm \sqrt{a^2m^2 - b^2} \sim$

@@  $k = \pm \frac{a}{m}$

@@  $k = \pm \sqrt{a^2m^2 + b^2}$

@@  $k = \pm \frac{a}{m} \sqrt{m^2 + 1}$

^^ The condition for the line  $y = mx + k$  to be a tangent to the conics  $y^2 = 4ax$  is

@@  $k = \pm\sqrt{a^2m^2 + b^2}$

@@  $k = \frac{a}{m} \sim$

@@  $k = \frac{m}{a}$

@@  $k = \pm\sqrt{a^2m^2 - b^2}$

# SECTION 4

^^ At the point  $(9, 6\sqrt{6})$  on the hyperbola  $\frac{x^2}{9} - \frac{y^2}{16} = 1$ , the equation of the tangent is

@@  $9x + 2\sqrt{6}y = 7$

@@  $3\sqrt{6}x + 2y = 4$

@@  $9x - 2\sqrt{6}y - 9 = 0 \sim$

@@  $9x + 27y - 6\sqrt{6} = 0$

^^ Tangents at two points  $P(8,8)$  and  $Q(2,4)$  on the Parabola  $x = 2t^2, y = 4t$  meet at  $R$ , the Coordinates of  $R$

@@  $(2, 1)$

@@  $(4, 6) \sim$

@@  $(3, 2)$

@@  $(0, 0)$

^^ Equation of tangent to the curve  $3x^2 + 6x - 12y = 0$  at  $P(2, 2)$  is \_\_\_\_\_

@@  $2y - 3x + 2 = 0 \sim$

@@  $3y + 2x - 10 = 0$

@@  $3y - 2x - 2 = 0$

@@  $2y + 3x - 10 = 0$

^^ Equation of tangent to the parabola  $y^2 = 12x$  at  $(0, 1)$  is

@@  $2y + x = 1$

@@  $y - x = 2$

@@  $y - 6x = 1$

@@  $6y = x - 1 \sim$

^^ A parabola has parametric equation  $x = t^2, y = 2t$ . What is the equation of its tangent if  $t = 2$ ?

@@  $y + 2x + 4 = 0$

@@  $y - 2x + 4 = 0$

@@  $2y - x - 4 = 0 \sim$

@@  $x - y - 4 = 0$

^^ The equation of tangent to the parabola  $x^2 = 4(y + 1)$  at the point  $P(2, -1)$

@@  $y = x + 1$

@@  $y = x - 3 \sim$

@@  $y = x - 1$

@@  $y = x + 3$

^^ The line tangent to the curve  $y = \sqrt{16-x}$  at the point  $(0, 4)$  has slope

@@ -8

@@ 4

@@  $-\frac{1}{8}$  ~

@@ 8

^^ Let  $x^2 + 4y^2 - 2x + 4y - 2 = 0$  be the equation of an ellipse. The slope of the tangent to this ellipse at  $(\frac{9}{5}, 4)$  is

@@  $\frac{4}{5}$

@@  $-\frac{5}{4}$  ~

@@  $-\frac{4}{5}$

@@  $\frac{5}{4}$

^^ Let  $x^2 + 4y^2 - 2x + 4y - 2 = 0$  be the equation of an ellipse. Equation of the tangent to the ellipse at  $(\frac{9}{5}, 4)$  is

@@  $5x + 4y = 25$  ~

@@  $4x + 5y = 9$

@@  $5x + 4y = 9$

@@  $4x + 5y = 25$

^^ The parametric equation of an ellipse is  $x = 4\cos \theta$ ,  $y = 3\sin \theta$ . If  $\theta = \frac{\pi}{3}$ , equation of the tangent to this ellipse is

@@  $\frac{x}{3} + \frac{y\sqrt{3}}{4} = 1$

@@  $\frac{x}{4} + \frac{y\sqrt{3}}{3} = 1$

@@  $\frac{x}{8} + \frac{y\sqrt{3}}{6} = 1$  ~

@@  $\frac{x}{6} + \frac{y\sqrt{3}}{8} = 1$

^^ At what point on the graph of  $y = \frac{1}{2}x^2$  is the tangent line parallel to the line  $2x - 4y = 3$  ?

@@  $(\frac{1}{2}, \frac{1}{2})$

@@  $(\frac{1}{2}, \frac{1}{8})$  ~

@@  $(1, -\frac{1}{4})$

@@  $\left(1, \frac{1}{2}\right)$

^^ The slope of the line tangent to the graph of  $y = \ln\left(\frac{x}{2}\right)$  at  $x = 6$  is:

@@  $\frac{1}{2}$

@@  $\frac{1}{4}$

@@  $\frac{1}{6} \sim$

@@  $\frac{1}{8}$

^^ An equation of the line tangent to  $y = x^3 + 3x^2 + 2$  at its point of inflexion is

@@  $y = -6x - 6$

@@  $y = 2x + 10$

@@  $y = 3x - 1$

@@  $y = -3x + 1 \sim$

^^ The line tangent to the curve  $y = \sqrt{36 - x}$  at the point  $(0, 4)$  has slope

@@  $-12$

@@  $6$

@@  $-\frac{1}{12} \sim$

@@  $12$

^^ The condition for the line  $y = mx + k$  to be a tangent to the conics

$$b^2x^2 + a^2y^2 = a^2b^2 \text{ is}$$

@@  $k = \pm\sqrt{a^2m^2 + b^2} \sim$

@@  $k = \pm\frac{a}{m}$

@@  $k = \pm\sqrt{a^2m^2 - b^2}$

@@  $k = \pm\frac{a}{m}\sqrt{m^2 + 1}$

^^ The slope of the tangent at any point on the rectangular hyperbola  $x = ct, y = ct^{-1}$  is

@@  $ct$

@@  $-t^{-2} \sim$

@@  $t^2$

@@  $-ct$

^^ The equation of tangent to the curve  $2x^2 + y^2 - xy = 2$  at the point  $(1, 1)$  is

@@  $y + 3x - 4 = 0 \sim$

@@  $3y + x + 4 = 0$

@@  $y - 3x - 4 = 0$

@@  $3x + y + 4 = 0$

^^ The equation of tangent to the curve  $x^2 = 4y$  at the point  $(2, 1)$  is

@@  $y + x = 1$

@@  $y - x = -3$

@@  $y - x = -1$  ~

@@  $x - y = 3$

^^ The line tangent to the curve  $y^2 = x + 4$  at the point  $(0, 2)$  is;

@@  $4y - x - 2 = 0$

@@  $4y - x - 8 = 0$  ~

@@  $4y + x - 8 = 0$

@@  $y - x - 2 = 0$

# SECTION 5

^^ The equation  $10x^2 - 10(y - 2)^2 - 1 = 0$  represents a/an

@@ rectangular hyperbola ~

@@ parabola

@@ ellipse

@@ hyperbola

^^ The equation  $2x^2 - 4(y - 2)^2 - 8 = 0$  represents a/an

@@ rectangular hyperbola

@@ parabola

@@ ellipse

@@ hyperbola ~

^^ The equation  $4x^2 + 12(y - 2)^2 - 48 = 0$  represents a/an

@@ rectangular hyperbola

@@ parabola

@@ ellipse ~

@@ hyperbola

^^ The equation  $4(x + 7)^2 + 12(y + 2)^2 - 48 = 0$  represents a/an

@@ rectangular hyperbola

@@ parabola

@@ ellipse ~

@@ hyperbola

^^ The equation  $x + 3(y + 2)^2 - 12 = 0$  represents a/an

@@ rectangular hyperbola

@@ parabola ~

@@ ellipse

@@ hyperbola

^^ The equation  $12x + (y + 2)^2 - 6 = 0$  represents a/an

@@ rectangular hyperbola

@@ parabola ~

@@ ellipse

@@ hyperbola

^^ The equation  $x^2 - (y + 2)^2 - 16 = 0$  represents a/an

@@ rectangular hyperbola ~  
 @@ parabola  
 @@ ellipse  
 @@ hyperbola  
 ^^ The equation  $x^2 + y^2 - 16 = 0$  represents a/an  
 @@ rectangular hyperbola  
 @@ circle ~  
 @@ ellipse  
 @@ hyperbola  
 ^^ The equation  $x^2 + y^2 - 1 = 0$  represents a/an  
 @@ rectangular hyperbola  
 @@ circle ~  
 @@ ellipse  
 @@ hyperbola  
 ^^ The equation  $x^2 + y^2 - 36 = 0$  represents a/an  
 @@ rectangular hyperbola  
 @@ circle ~  
 @@ ellipse  
 @@ hyperbola

# SECTION 6

^^ The values of  $x$  at the stationary points of the function  $y = 4x^3 + 15x^2 - 18x + 7$  are  
 @@  $x = \frac{1}{2}$  and  $x = -3$  ~  
 @@  $x = \frac{1}{3}$  and  $x = 3$   
 @@  $x = \frac{1}{5}$  and  $x = 2$   
 @@  $x = \frac{1}{3}$  and  $x = -2$   
 ^^ The values of  $x$  at the stationary points of the function  $y = x^3 - 3x^2 + 3x + 2$  are  
 @@  $x = 1$  and  $x = 1$  ~  
 @@  $x = -1$  and  $x = 3$   
 @@  $x = 1$  and  $x = 2$   
 @@  $x = -2$  and  $x = 2$   
 ^^ The values of  $x$  at the stationary points of the function  $y = x^3 - 3x - 2$  are  
 @@  $x = 1$  and  $x = -1$  ~  
 @@  $x = -1$  and  $x = 3$   
 @@  $x = 1$  and  $x = 2$   
 @@  $x = 1$  and  $x = 1$   
 ^^ The values of  $x$  at the stationary points of the function  $y = 2x^3 + 3x^2 + 36x + 5$  are

@@  $x = -3$  and  $x = 2$  ~

@@  $x = -1$  and  $x = 3$

@@  $x = 1$  and  $x = 2$

@@  $x = -2$  and  $x = 2$

^^ The values of  $x$  at the stationary points of the function  $y = 3x^3 - 2x^2 - 5x - 5$  are

@@  $x = 1$  and  $x = -\frac{5}{9}$  ~

@@  $x = -1$  and  $x = -\frac{4}{9}$

@@  $x = 1$  and  $x = \frac{5}{9}$

@@  $x = -2$  and  $x = 2$

^^ The values of  $x$  at the stationary points of the function  $y = x^3 - 3x^2 + 3x$  are

@@  $x = 1$  and  $x = 1$  ~

@@  $x = -1$  and  $x = 3$

@@  $x = 1$  and  $x = 2$

@@  $x = -2$  and  $x = 2$

^^ The values of  $x$  at the stationary points of the function  $y = 2x^3 - 3x^2 - 12x + 1$  are

@@  $x = 2$  and  $x = -1$  ~

@@  $x = -1$  and  $x = 3$

@@  $x = 1$  and  $x = 2$

@@  $x = -2$  and  $x = 2$

^^ The values of  $x$  at the stationary points of the function  $y = x^3 - 2x^2 + x + 4$  are

@@  $x = \frac{1}{3}$  and  $x = 1$  ~

@@  $x = -1$  and  $x = 3$

@@  $x = \frac{1}{3}$  and  $x = 2$

@@  $x = -2$  and  $x = 2$

^^ The values of  $x$  at the stationary points of the function  $y = x^3 - 6x^2 + 9x + 1$  are

@@  $x = 3$  and  $x = 1$  ~

@@  $x = -1$  and  $x = 3$

@@  $x = \frac{1}{3}$  and  $x = 2$

@@  $x = -2$  and  $x = 2$

## SECTION 7

^^ Given that  $y = x^3 - 6x^2 + 9x + 1$ , the value of  $x$  at the inflexion point is  $x = \frac{5}{6}$

@@ True ~

@@ False

^^ Given that  $y = x^3 - 6x^2 + 9x + 1$ , the value of  $x$  at the inflexion point is  $x = \frac{6}{5}$

@@ True

@@ False ~

^^ At a local minimum,  $\frac{dy}{dx}$  changes from positive to negative as x increases

@@ True

@@ False ~

^^ At a local maximum,  $\frac{dy}{dx}$  changes from positive to negative as x increases

@@ True ~

@@ False

^^ At a local minimum,  $\frac{dy}{dx}$  changes from negative to positive as x increases

@@ True ~

@@ False

^^ At a local maximum,  $\frac{dy}{dx}$  changes from negative to positive as x increases

@@ True

@@ False ~

^^ At the point of inflexion of the function y,  $\frac{d^2y}{dx^2} > 0$

@@ True

@@ False ~

^^ At the point of inflexion of the function y,  $\frac{d^2y}{dx^2} < 0$

@@ True

@@ False ~

^^ At the point of inflexion of the function y,  $\frac{d^2y}{dx^2} = 0$

@@ True ~

@@ False

^^ The function  $y = 2x^3 - 5x^2 - 4x + 1$  is minimum at  $x = 2$

@@ True ~

@@ False

^^ At a minimum point of the function y,  $\frac{d^2y}{dx^2} < 0$

@@ True

@@ False ~

^^ The function  $y = 2x^3 - 5x^2 - 4x + 1$  is maximum at  $x = 2$

@@ True

@@ False ~

^^ The function  $y = x^3 - 2x^2 + x + 3$  is maximum at  $x = 1$

@@ True

@@ False ~

^^ The function  $y = 2x^3 - 2x^2 + x + 3$  is maximum at  $x = \frac{1}{3}$

@@ True ~

@@ False

^^ At a maximum point of the function  $y$ ,  $\frac{d^2y}{dx^2} < 0$

@@ True ~

@@ False

^^ At a maximum point of the function  $y$ ,  $\frac{d^2y}{dx^2} > 0$

@@ True

@@ False ~

# SECTION 8

^^ The function  $y = x^3$  has an extremum value at  $x = 0$ . What is the nature of the extremum value ?

@@ a maximum

@@ a minimum

@@ point of inflexion ~

@@ local minimum

^^ A cuboid with volume  $V = (10 - 2x) \times (10 - 2x) \times x$  is formed from a sheet of paper  $10\text{cm} \times 10\text{cm}$ . What is the maximum volume that this cuboid can ever have?

@@  $74\frac{2}{27} \text{cm}^3$  ~

@@  $50\frac{1}{2} \text{cm}^3$

@@  $96 \text{cm}^3$

@@  $100 \text{cm}^3$

^^ If  $y = t^3 - 3t + 2$ . Find the maximum value of  $t$ .

@@ -1

@@ 2

@@ 4 ~

@@ 1

^^ A stone is thrown vertically upwards from the top of a cliff  $60\text{cm}$  at  $20\text{m/s}$ . find the maximum height attained by the stone ( taking  $g = 10\text{cm/s}^2$  )

@@  $20\text{cm}$

@@  $40\text{cm}$

@@  $60\text{cm}$

@@  $80\text{cm}$  ~

^^ A cuboid with volume  $V = (10 - 2x) \times (10 - 2x) \times x$  is formed from a sheet of paper  $10\text{cm} \times 10\text{cm}$ . For what value of  $x$  does the cuboid has its minimum volume.

- @@ 2cm
- @@ 3cm
- @@ 4cm
- @@ 5cm ~

^^ A cuboid with volume  $V = (10 - 2x) \times (10 - 2x) \times x$  is formed from a sheet of paper  $10\text{cm} \times 10\text{cm}$ . What is the minimum volume that this cuboid can ever have?

- @@  $4\text{ cm}^3$
- @@  $0\text{ cm}^3$  ~
- @@  $2\text{ cm}^3$
- @@  $3\text{ cm}^3$

^^ If  $y = x^3 - 3x + 2$ . The minimum value of  $y$  is:

- @@ -1
- @@ 2
- @@ 0 ~
- @@ 1

^^ The cost  $T$  of a product is a function of the quantity  $x$  of the product is given by the relation:  $T(x) = 2x^2 - 4000x + 50$ . Find the quantity for which the cost is a minimum.

- @@ 4000
- @@ 2000
- @@ 1500
- @@ 1000 ~

^^ The function  $y = x^4 - 4x^3 + 10$  has a minimum value in the interval  $0 \leq x \leq 5$ . The coordinates of the minimum point is

- @@ (2, -6)
- @@ (1.8, 0)
- @@ (3.8, 0)
- @@ (3, -17) ~

^^ The function  $y = x^4 - 4x^3 + 10$  has a minimum value in the interval  $-2 \leq x \leq 2$ . The coordinates of the point of inflexion

- @@ (2, 10)
- @@ (0, 10) ~
- @@ (1, 10)
- @@ (-2, 10)

^^ The coordinate of the turning points of the curve  $y = x^3 - 3x + 2$  are:

- @@ (-1, 4) and (1, 0) ~
- @@ (-1, 0) and (1, 4)
- @@ (4, -1) and (0, 1)
- @@ (-1, 1) and (0, 4)

# SECTION 9

^^ The conic represented by the equations  $x = -1 + 5\cos\theta$  and  $y - 2 = 4\sin\theta$  is

@@  $\frac{(x + 1)^2}{25} + \frac{(y - 2)^2}{16} = 1 \sim$

@@  $\frac{(x + 1)^2}{25} - \frac{(y - 2)^2}{16} = 1$

@@  $\frac{(x + 1)^2}{25} + \frac{(y + 2)^2}{16} = 1$

@@  $\frac{(x - 1)^2}{25} + \frac{(y - 2)^2}{16} = 1$

^^ The conic represented by the equations  $x = 1 + 6\cos\theta$  and  $y - 2 = 4\sin\theta$  is

@@  $\frac{(x - 1)^2}{36} + \frac{(y - 2)^2}{16} = 1 \sim$

@@  $\frac{(x + 1)^2}{36} - \frac{(y - 2)^2}{16} = 1$

@@  $\frac{(x + 1)^2}{36} + \frac{(y + 2)^2}{16} = 1$

@@  $\frac{(x - 1)^2}{36} - \frac{(y - 2)^2}{16} = 1$

^^ The conic represented by the equations  $x = -3 + 5\cos\theta$  and  $y - 2 = 4\sin\theta$  is

@@  $\frac{(x + 3)^2}{25} + \frac{(y - 2)^2}{16} = 1 \sim$

@@  $\frac{(x + 3)^2}{25} - \frac{(y - 2)^2}{16} = 1$

@@  $\frac{(x + 3)^2}{25} + \frac{(y + 2)^2}{16} = 1$

@@  $\frac{(x - 3)^2}{25} + \frac{(y - 2)^2}{16} = 1$

^^ The conic represented by the equations  $x = -1 + 5\cos\theta$  and  $y - 7 = 4\sin\theta$  is

@@  $\frac{(x + 1)^2}{25} + \frac{(y - 7)^2}{16} = 1 \sim$

@@  $\frac{(x + 1)^2}{25} - \frac{(y - 7)^2}{16} = 1$

@@  $\frac{(x + 1)^2}{25} + \frac{(y + 7)^2}{16} = 1$

@@  $\frac{(x - 1)^2}{25} + \frac{(y - 7)^2}{16} = 1$

^^ The conic represented by the equations  $x = -1 + 5\cos\theta$  and  $y - 2 = 6\sin\theta$  is

$$@@ \frac{(x+1)^2}{25} + \frac{(y-2)^2}{36} = 1 \sim$$

$$@@ \frac{(x+1)^2}{25} - \frac{(y-2)^2}{36} = 1$$

$$@@ \frac{(x+1)^2}{25} + \frac{(y+2)^2}{36} = 1$$

$$@@ \frac{(x-1)^2}{25} + \frac{(y-2)^2}{36} = 1$$

^^ The conic represented by the equations  $x = 2 + 5\cos\theta$  and  $y = 2 + 6\sin\theta$  is

$$@@ \frac{(x-2)^2}{25} + \frac{(y-2)^2}{36} = 1 \sim$$

$$@@ \frac{(x+2)^2}{25} - \frac{(y-2)^2}{36} = 1$$

$$@@ \frac{(x+1)^2}{25} + \frac{(y+2)^2}{36} = 1$$

$$@@ \frac{(x-1)^2}{25} + \frac{(y-2)^2}{36} = 1$$

^^ The conic represented by the equations  $x = 2 + 3\cos\theta$  and  $y = 2 + 2\sin\theta$  is

$$@@ \frac{(x-2)^2}{9} + \frac{(y-2)^2}{4} = 1 \sim$$

$$@@ \frac{(x+2)^2}{9} - \frac{(y-2)^2}{4} = 1$$

$$@@ \frac{(x+1)^2}{9} + \frac{(y+2)^2}{4} = 1$$

$$@@ \frac{(x-1)^2}{9} + \frac{(y-2)^2}{4} = 1$$

^^ The conic represented by the equations  $x = -2 + 5\cos\theta$  and  $y = 2 + 2\sin\theta$  is

$$@@ \frac{(x+2)^2}{25} + \frac{(y-2)^2}{4} = 1 \sim$$

$$@@ \frac{(x+2)^2}{25} - \frac{(y-2)^2}{4} = 1$$

$$@@ \frac{(x+2)^2}{25} + \frac{(y+2)^2}{4} = 1$$

$$@@ \frac{(x-2)^2}{25} + \frac{(y-2)^2}{4} = 1$$

^^ The conic represented by the equations  $x = -4 + 5\cos\theta$  and  $y = 2 + 6\sin\theta$  is

$$@@ \frac{(x+4)^2}{25} + \frac{(y-2)^2}{36} = 1 \sim$$

$$@@ \frac{(x+4)^2}{25} - \frac{(y-2)^2}{36} = 1$$

$$@@ \frac{(x+4)^2}{25} + \frac{(y+2)^2}{36} = 1$$

$$@@ \frac{(x-4)^2}{25} + \frac{(y-2)^2}{36} = 1$$

^^ The conic represented by the equations  $x = -4 + 5\cos\theta$  and  $y = 5 + 6\sin\theta$  is

$$@@ \frac{(x+4)^2}{25} + \frac{(y-5)^2}{36} = 1 \sim$$

$$@@ \frac{(x+4)^2}{25} - \frac{(y-5)^2}{36} = 1$$

$$@@ \frac{(x+4)^2}{25} + \frac{(y+5)^2}{36} = 1$$

$$@@ \frac{(x-4)^2}{25} + \frac{(y-5)^2}{36} = 1$$

# SECTION 10

^^ The conic represented by the equations  $x = -1 + 5\sec\theta$  and  $y - 2 = 4\tan\theta$  is

$$@@ \frac{(x+1)^2}{25} - \frac{(y-2)^2}{16} = 1 \sim$$

$$@@ \frac{(x+1)^2}{25} + \frac{(y-2)^2}{16} = 1$$

$$@@ \frac{(x+1)^2}{25} + \frac{(y+2)^2}{16} = 1$$

$$@@ \frac{(x-1)^2}{25} + \frac{(y-2)^2}{16} = 1$$

^^ The conic represented by the equations  $x = 1 + 6\sec\theta$  and  $y - 2 = 4\tan\theta$  is

$$@@ \frac{(x-1)^2}{36} - \frac{(y-2)^2}{16} = 1 \sim$$

$$@@ \frac{(x+1)^2}{36} - \frac{(y-2)^2}{16} = 1$$

$$@@ \frac{(x+1)^2}{36} + \frac{(y+2)^2}{16} = 1$$

$$@@ \frac{(x+1)^2}{36} - \frac{(y-2)^2}{16} = 1$$

^^ The conic represented by the equations  $x = -3 + 5\sec\theta$  and  $y - 2 = 4\tan\theta$  is

$$@@ \frac{(x+3)^2}{25} - \frac{(y-2)^2}{16} = 1 \sim$$

$$@@ \frac{(x+3)^2}{25} + \frac{(y-2)^2}{16} = 1$$

$$@@ \frac{(x+3)^2}{25} + \frac{(y+2)^2}{16} = 1$$

$$@@ \frac{(x-3)^2}{25} + \frac{(y-2)^2}{16} = 1$$

^^ The conic represented by the equations  $x = -1 + 5\sec\theta$  and  $y - 7 = 4\tan\theta$  is

$$@@ \frac{(x+1)^2}{25} - \frac{(y-7)^2}{16} = 1 \sim$$

$$@@ \frac{(x+1)^2}{25} + \frac{(y-7)^2}{16} = 1$$

$$@@ \frac{(x+1)^2}{25} + \frac{(y+7)^2}{16} = 1$$

$$@@ \frac{(x-1)^2}{25} + \frac{(y-7)^2}{16} = 1$$

^^ The conic represented by the equations  $x = -1 + 5\sec\theta$  and  $y - 2 = 6\tan\theta$  is

$$@@ \frac{(x+1)^2}{25} - \frac{(y-2)^2}{36} = 1 \sim$$

$$@@ \frac{(x+1)^2}{25} + \frac{(y-2)^2}{36} = 1$$

$$@@ \frac{(x+1)^2}{25} - \frac{(y+2)^2}{36} = 1$$

$$@@ \frac{(x-1)^2}{25} + \frac{(y-2)^2}{36} = 1$$

^^ The conic represented by the equations  $x = 2 + 5\sec\theta$  and  $y = 2 + 6\tan\theta$  is

$$@@ \frac{(x-2)^2}{25} - \frac{(y-2)^2}{36} = 1 \sim$$

$$@@ \frac{(x+2)^2}{25} - \frac{(y-2)^2}{36} = 1$$

$$@@ \frac{(x+1)^2}{25} + \frac{(y+2)^2}{36} = 1$$

$$@@ \frac{(x-1)^2}{25} + \frac{(y-2)^2}{36} = 1$$

^^ The conic represented by the equations  $x = 2 + 3\sec\theta$  and  $y = 2 + 2\tan\theta$  is

$$@@ \frac{(x-2)^2}{9} - \frac{(y-2)^2}{4} = 1 \sim$$

$$@@ \frac{(x+2)^2}{9} - \frac{(y-2)^2}{4} = 1$$

$$@@ \frac{(x+1)^2}{9} + \frac{(y+2)^2}{4} = 1$$

$$@@ \frac{(x-1)^2}{9} + \frac{(y-2)^2}{4} = 1$$

^^ The conic represented by the equations  $x = -2 + 5\sec\theta$  and  $y = 2 + 2\tan\theta$  is

@@  $\frac{(x+2)^2}{25} - \frac{(y-2)^2}{4} = 1$  ~

@@  $\frac{(x+2)^2}{25} + \frac{(y-2)^2}{4} = 1$

@@  $\frac{(x+2)^2}{25} + \frac{(y+2)^2}{4} = 1$

@@  $\frac{(x-2)^2}{25} - \frac{(y-2)^2}{4} = 1$

^^ The conic represented by the equations  $x = -4 + 5\sec\theta$  and  $y = 2 + 6\tan\theta$  is

@@  $\frac{(x+4)^2}{25} - \frac{(y-2)^2}{36} = 1$  ~

@@  $\frac{(x+4)^2}{25} + \frac{(y-2)^2}{36} = 1$

@@  $\frac{(x+4)^2}{25} - \frac{(y+2)^2}{36} = 1$

@@  $\frac{(x-4)^2}{25} + \frac{(y-2)^2}{36} = 1$

^^ The conic represented by the equations  $x = -4 + 5\sec\theta$  and  $y = 5 + 6\tan\theta$  is

@@  $\frac{(x+4)^2}{25} - \frac{(y-5)^2}{36} = 1$  ~

@@  $\frac{(x+4)^2}{25} + \frac{(y-5)^2}{36} = 1$

@@  $\frac{(x+4)^2}{25} + \frac{(y+5)^2}{36} = 1$

@@  $\frac{(x-4)^2}{25} - \frac{(y-5)^2}{36} = 1$

# SECTION 11

^^ The conic represented by the equations  $x = 4t^2$  and  $y = 8t$  is

@@  $y^2 = 16x$  ~

@@  $y^2 = 8x$

@@  $y^2 = 4x$

@@  $y^2 = -16x$

^^ The conic represented by the equations  $x = 6t^2$  and  $y = 12t$  is

@@  $y^2 = 24x$  ~

@@  $y^2 = 12x$

@@  $y^2 = 6x$

$$@@ y^2 = -24x$$

^^ The conic represented by the equations  $x = 5t^2$  and  $y = 10t$  is

$$@@ y^2 = 20x \sim$$

$$@@ y^2 = 10x$$

$$@@ y^2 = 5x$$

$$@@ y^2 = -20x$$

^^ The conic represented by the equations  $x = 8t^2$  and  $y = 16t$  is

$$@@ y^2 = 32x \sim$$

$$@@ y^2 = 16x$$

$$@@ y^2 = 8x$$

$$@@ y^2 = -32x$$

^^ The conic represented by the equations  $x = 3t^2$  and  $y = 6t$  is

$$@@ y^2 = 12x \sim$$

$$@@ y^2 = 6x$$

$$@@ y^2 = 3x$$

$$@@ y^2 = -12x$$

^^ The conic represented by the equations  $x = 7t^2$  and  $y = 14t$  is

$$@@ y^2 = 28x \sim$$

$$@@ y^2 = 14x$$

$$@@ y^2 = 7x$$

$$@@ y^2 = -28x$$

^^ The conic represented by the equations  $x = 9t^2$  and  $y = 18t$  is

$$@@ y^2 = 36x \sim$$

$$@@ y^2 = 18x$$

$$@@ y^2 = 9x$$

$$@@ y^2 = -36x$$

^^ The conic represented by the equations  $x = 11t^2$  and  $y = 22t$  is

$$@@ y^2 = 44x \sim$$

$$@@ y^2 = 22x$$

$$@@ y^2 = 11x$$

$$@@ y^2 = -44x$$

^^ The conic represented by the equations  $x = t^2$  and  $y = 2t$  is

$$@@ y^2 = 4x \sim$$

$$@@ y^2 = 2x$$

$$@@ y^2 = x$$

$$@@ y^2 = -4x$$

^^ The conic represented by the equations  $x = 0.5t^2$  and  $y = t$  is

$$@@ y^2 = 2x \sim$$

$$@@ y^2 = x$$

$$@@ y^2 = 0.5x$$

$$@@ y^2 = -2x$$

# SECTION 12

^^ The degree of the differential equation  $\frac{d^3y}{dx^3} - 8x\left(\frac{dy}{dx}\right) = y\frac{d^2y}{dx^2} + e^y$  is

@@ 1 ~

@@ 2

@@ 3

@@ 4

^^ Classify the following differential equation:  $e^{2x}\frac{dy}{dx} - 2y = x^3y$

@@ separable and not linear

@@ linear and not separable

@@ both separable and linear ~

@@ neither separable nor linear

^^ Classify the following differential equation:  $e^{2x}\frac{dy}{dx} - 2y^2 = x^3y^2$

@@ separable and not linear ~

@@ linear and not separable

@@ both separable and linear

@@ neither separable nor linear

^^ An integrating factor,  $I(x)$ , for the linear differential equation  $(1 + x^2)\frac{dy}{dx} + xy = 0$

@@  $I(x) = e^{\frac{x^2}{2}}$

@@  $I(x) = 1 + x^2$

@@  $I(x) = \sqrt{1 + x^2}$  ~

@@  $I(x) = e^{\frac{1+x^2}{2}}$

^^ The order of the differential equation  $\frac{d^3y}{dx^3} + 4x\left(\frac{dy}{dx}\right)^3 = y\frac{d^2y}{dx^2} + e^y$  is

@@ 1

@@ 2

@@ 3 ~

@@ 4

^^ The order of the differential equation  $\frac{d^5y}{dx^5} + 4x\left(\frac{dy}{dx}\right)^3 = y\frac{d^2y}{dx^2} + e^y$  is

@@ 3

@@ 2

@@ 5 ~

@@ 4

^^ Consider the linear ordinary differential equation  $\frac{dy}{dx} - \frac{2x}{1+x^2}y = 1+x$ . The integrating

factor is:

@@  $\frac{1}{1+x^2}$  ~

@@  $1+x^2$

@@  $e^{(1+x^2)}$

@@  $e^{-(1+x^2)}$

^^ Consider the linear ordinary differential equation  $x\frac{dy}{dx} - y = 1$ . The integrating factor is:

@@  $\frac{1}{x}$  ~

@@  $1+x$

@@  $e^{(1+x^2)}$

@@  $e^{-(1+x^2)}$

^^ Classify the following differential equation:  $w\frac{dw}{dx} + 3t = 10$

@@ separable and not linear ~

@@ linear and not separable

@@ both separable and linear

@@ neither separable nor linear

^^ Find the differential of  $y = x^2 - 2x + 2$  if  $x$  changes from 3.0 to 3.2

@@ 0.7

@@ 0.9

@@ 0.8 ~

@@ 0.6

^^ The degree of the differential equation  $\frac{d^3y}{dx^3} + 6x\left(\frac{dy}{dx}\right) = y\frac{d^2y}{dx^2} + e^y$  is

@@ 1 ~

@@ 2

@@ 3

@@ 4

^^ The degree of the differential equation  $\left(\frac{d^3y}{dx^3}\right)^2 - 8x\left(\frac{dy}{dx}\right) = y\frac{d^2y}{dx^2} + e^y$  is

@@ 2 ~

@@ 1

@@ 3

@@ 4

# SECTION 13

^^An ellipse has a major axis of 20 and a minor axis of 12. A possible equation for this ellipse is:

@@  $\frac{x^2}{100} + \frac{y^2}{36} = 1$  ~

@@  $\frac{x^2}{400} + \frac{y^2}{144} = 1$

@@  $\frac{x^2}{100} + \frac{y^2}{144} = 1$

@@  $\frac{x^2}{400} + \frac{y^2}{36} = 1$

^^An ellipse has a major axis of 10 and a minor axis of 8. A possible equation for this ellipse is:

@@  $\frac{x^2}{25} + \frac{y^2}{16} = 1$  ~

@@  $\frac{x^2}{100} + \frac{y^2}{64} = 1$

@@  $\frac{x^2}{10} + \frac{y^2}{8} = 1$

@@  $\frac{x^2}{400} + \frac{y^2}{36} = 1$

^^An ellipse has a major axis of 20 and a minor axis of 10. A possible equation for this ellipse is:

@@  $\frac{x^2}{100} + \frac{y^2}{25} = 1$  ~

@@  $\frac{x^2}{400} + \frac{y^2}{100} = 1$

@@  $\frac{x^2}{100} + \frac{y^2}{10} = 1$

$$@@ \frac{x^2}{400} + \frac{y^2}{20} = 1$$

^^An ellipse has a major axis of 16 and a minor axis of 12. A possible equation for this ellipse is:

$$@@ \frac{x^2}{64} + \frac{y^2}{36} = 1 \sim$$

$$@@ \frac{x^2}{16} + \frac{y^2}{12} = 1$$

$$@@ \frac{x^2}{100} + \frac{y^2}{144} = 1$$

$$@@ \frac{x^2}{400} + \frac{y^2}{36} = 1$$

^^An ellipse has a major axis of 18 and a minor axis of 10. A possible equation for this ellipse is:

$$@@ \frac{x^2}{81} + \frac{y^2}{25} = 1 \sim$$

$$@@ \frac{x^2}{18} + \frac{y^2}{25} = 1$$

$$@@ \frac{x^2}{18} + \frac{y^2}{100} = 1$$

$$@@ \frac{x^2}{400} + \frac{y^2}{36} = 1$$

^^An ellipse has a major axis of 40 and a minor axis of 12. A possible equation for this ellipse is:

$$@@ \frac{x^2}{200} + \frac{y^2}{36} = 1 \sim$$

$$@@ \frac{x^2}{400} + \frac{y^2}{144} = 1$$

$$@@ \frac{x^2}{40} + \frac{y^2}{12} = 1$$

$$@@ \frac{x^2}{400} + \frac{y^2}{36} = 1$$

^^An ellipse has a major axis of 22 and a minor axis of 12. A possible equation for this ellipse is:

$$@@ \frac{x^2}{121} + \frac{y^2}{36} = 1 \sim$$

$$@@ \frac{x^2}{242} + \frac{y^2}{144} = 1$$

$$@@ \frac{x^2}{22} + \frac{y^2}{12} = 1$$

$$@@ \frac{x^2}{400} + \frac{y^2}{144} = 1$$

## SECTION 14

^^ If  $y^2 - 2y - 8x - 7 = 0$  is a parabolic equation then the focus is

$$@@ (1, 0)$$

$$@@ (0, 1)$$

$$@@ (-1, -1)$$

$$@@ (1, 1) \sim$$

^^ The equation of a parabola when the focus is at  $(4, 0)$  and vertex  $(1, 0)$  is given as

$$@@ y^2 = 8(x+1)$$

$$@@ (y-1)^2 = 12x$$

$$@@ y^2 = 12(x-1) \sim$$

$$@@ y^2 = 8(x-1)$$

^^ The focus and directrix of the parabola  $y^2 = 9x$  are

$$@@ \left(\frac{9}{4}, 0\right) \text{ and } -\frac{9}{4} \sim$$

$$@@ \left(\frac{9}{4}, 0\right) \text{ and } -\frac{9}{4}$$

$$@@ \left(\frac{9}{4}, 0\right) \text{ and } -\frac{9}{4}$$

$$@@ \left(\frac{9}{4}, 0\right) \text{ and } -\frac{9}{4}$$

^^ The equation of the parabola with focus  $\left(0, -\frac{1}{2}\right)$  and directrix  $\frac{1}{2}$  is

$$@@ y^2 = -4x$$

@@  $x^2 = -2y$  ~

@@  $x^2 = 4y$

@@  $y^2 = -2x$

^^ Given that focus:  $(4, 0)$  and directrix:  $x = -4$ , then the equation of the parabola is

@@  $y^2 = -16x$

@@  $x^2 = -16y$

@@  $y^2 = 16x$  ~

@@  $y^2 = 8x$

^^ Find the equation of the parabola with vertex at the origin and focus  $(6, 0)$

@@  $x^2 = 24y$

@@  $y^2 = -24x$

@@  $y^2 = 24x$  ~

@@  $x^2 = -24y$

^^ Find the focus of the equation  $x^2 + 3y = 0$

@@  $\left(0, \frac{4}{3}\right)$

@@  $\left(-\frac{3}{4}, 0\right)$

@@  $\left(0, -\frac{3}{4}\right)$  ~

@@  $\left(-\frac{4}{3}, 0\right)$

^^ What is the required parabolic equation with focus  $\left(0, -\frac{1}{2}\right)$  and the directrix:  $y = \frac{1}{2}$

@@  $y^2 = 4x$

@@  $y^2 = -4x$

@@  $x^2 = 2y$

@@  $x^2 = -2y$  ~

^^ The focus of the parabola  $y^2 = 80x$  is

@@  $(0, 10)$

@@  $(-20, 0)$

$$@@ (20, 0) \sim$$

$$@@ (0, -10)$$

^^ The focus and directrix of the parabola  $x^2 = 9y$  respectively are

$$@@ \left( \frac{9}{4}, 0 \right) \text{ and } \frac{9}{4} \sim$$

$$@@ \left( 0, \frac{9}{4} \right) \text{ and } -\frac{9}{4}$$

$$@@ \left( 0, -\frac{9}{4} \right) \text{ and } \frac{9}{4}$$

$$@@ \left( -\frac{9}{4}, 0 \right) \text{ and } -\frac{9}{4}$$

^^ The focus and directrix of the parabola  $x^2 = -9y$  respectively are

$$@@ \left( -\frac{9}{4}, 0 \right) \text{ and } -\frac{9}{4}$$

$$@@ \left( \frac{9}{4}, 0 \right) \text{ and } \frac{9}{4}$$

$$@@ \left( 0, -\frac{9}{4} \right) \text{ and } \frac{9}{4} \sim$$

$$@@ \left( 0, \frac{9}{4} \right) \text{ and } -\frac{9}{4}$$

^^ The focus and directrix of the parabola  $y^2 = -9x$  respectively are

$$@@ \left( -\frac{9}{4}, 0 \right) \text{ and } \frac{9}{4} \sim$$

$$@@ \left( 0, -\frac{9}{4} \right) \text{ and } -\frac{9}{4}$$

$$@@ \left( 0, -\frac{9}{4} \right) \text{ and } \frac{9}{4}$$

$$@@ \left( \frac{9}{4}, 0 \right) \text{ and } -\frac{9}{4}$$

^^ The focus and directrix of the parabola  $y^2 = 4x$  respectively are

$$@@ (-4, 0) \text{ and } 4$$

$$@@ (-1, 0) \text{ and } 1$$

$$@@ (4, 0) \text{ and } -4$$

@@ (1, 0) and -1 ~

^^ The focus and directrix of the parabola  $y^2 = -4x$  respectively are

@@ (-1, 0) and 1 ~

@@ (-4, 0) and 4

@@ (1, 0) and -1

@@ (4, 0) and -4

^^ Given that focus (-4, 0) and directrix  $x = 4$ , then the equation of the parabola is

@@  $y^2 = 16x$

@@  $y^2 = -16x$  ~

@@  $x^2 = -16y$

@@  $x^2 = 16y$

^^ Given that focus (0, -4) and directrix  $y = 4$ , then the equation of the parabola is

@@  $y^2 = 16x$

@@  $y^2 = -16x$

@@  $x^2 = 16y$

@@  $x^2 = -16y$  ~

^^ Given that focus  $\left(0, \frac{1}{2}\right)$  and directrix  $y = -\frac{1}{2}$ , then the equation of the parabola is

@@  $x^2 = \frac{1}{2}x$

@@  $x^2 = -\frac{1}{2}y$

@@  $x^2 = 2y$  ~

@@  $y^2 = 2x$

^^ Given that focus  $\left(-\frac{1}{2}, 0\right)$  and directrix  $x = \frac{1}{2}$ , then the equation of the parabola is

@@  $y^2 = -2x$  ~

@@  $x^2 = -2y$

@@  $x^2 = 2y$

@@  $y^2 = 2x$

^^ Given that focus (0, 4) and directrix  $y = -4$ , then the equation of the parabola is

@@  $x^2 = 16y$  ~

@@  $y^2 = -16x$

@@  $y^2 = 16x$

@@  $x^2 = -16y$

^^ The focus of the equation  $x^2 - 3y = 0$  is

@@  $\left(0, \frac{3}{4}\right)$  ~

@@  $\left(0, -\frac{3}{4}\right)$

@@  $\left(0, \frac{4}{3}\right)$

@@  $\left(0, -\frac{4}{3}\right)$

^^ The focus of the equation  $y^2 + 3x = 0$  is

@@  $\left(0, \frac{3}{4}\right)$

@@  $\left(-\frac{3}{4}, 0\right)$  ~

@@  $\left(\frac{4}{3}, 0\right)$

@@  $\left(0, -\frac{4}{3}\right)$

^^ The focus of the equation  $y^2 - 3x = 0$  is

@@  $\left(-\frac{3}{4}, 0\right)$

@@  $\left(0, \frac{3}{4}\right)$

@@  $\left(\frac{3}{4}, 0\right)$  ~

@@  $\left(0, -\frac{3}{4}\right)$

^^ The focus of the equation  $x^2 - 24y = 0$  is

@@  $(6, 0)$

@@ (0, -6)

@@ (0, 6) ~

@@ (-6, 0)

^^ The focus of the equation  $y^2 + 24x = 0$  is

@@ (0, 6)

@@ (0, -6)

@@ (-6, 0) ~

@@ (6, 0)

## SECTION 15

^^ If the latus rectum of a parabola is  $\frac{\sqrt{7}}{3}$ , its focal length is

@@  $\frac{\sqrt{3}}{12}$  ~

@@  $\frac{12}{\sqrt{3}}$

@@  $-\frac{\sqrt{3}}{12}$

@@  $-\frac{12}{\sqrt{3}}$

^^ If the latus rectum of a parabola is  $\frac{7}{\sqrt{3}}$ , its focal length is

@@  $\frac{4\sqrt{3}}{7}$

@@  $\frac{7}{4\sqrt{3}}$  ~

@@  $-\frac{7}{4\sqrt{3}}$

@@  $-\frac{4\sqrt{3}}{7}$

^^ If the latus rectum of a parabola is 4, its focal length is

@@ 4

@@ -4

@@ 1 ~

@@ -1

^^ If the latus rectum of a parabola is  $\frac{1}{\sqrt{2}}$ , its focal length is

@@  $4\sqrt{2}$

@@  $-\frac{1}{4\sqrt{2}}$

@@  $-4\sqrt{2}$

@@  $\frac{1}{4\sqrt{2}}$  ~

^^ If the latus rectum of a parabola is  $\frac{\sqrt{3}}{2}$ , its focal length is

@@  $\frac{\sqrt{3}}{8}$  ~

@@  $\frac{8}{\sqrt{3}}$

@@  $-\frac{\sqrt{3}}{8}$

@@  $-\frac{8}{\sqrt{3}}$

^^ The length of latus rectum of the parabola  $x^2 - 6x - 2y + 5 = 0$  is

@@ 2 ~

@@ 4

@@ -4

@@ -2

^^ If the latus rectum of a parabola is  $\frac{3}{\sqrt{7}}$ , its focal length is

@@  $-\frac{4\sqrt{7}}{3}$

@@  $\frac{12}{\sqrt{7}}$

@@  $-\frac{\sqrt{7}}{3}$

$$@@ \frac{3}{4\sqrt{7}} \sim$$

^^ The length of the latus rectum of the parabola  $y^2 + 12y + 8x + 20 = 0$  is

@@ 8 ~

@@ 4

@@ 2

@@ -8

^^ A parabola with length of latus rectum  $\frac{1}{6}$  and vertex  $(0, -1)$  is given as

@@  $6(y+1)^2 = -x$  ~

@@  $(y+1)^2 = -6x$

@@  $(y-1)^2 = 6x$

@@  $6(y-1)^2 = x$

^^ If the latus rectum of a parabola is  $-4$  its focal length is

@@ 1

@@ -1 ~

@@ 4

@@ -4

^^ The length of latus rectum of the parabola  $x^2 - 2x - y + 6 = 0$  is

@@ 1 ~

@@ 2

@@ 3

@@ 4

^^ The length of latus rectum of the parabola  $y^2 - 7y - 7x + 3 = 0$  is

@@ 5

@@ 7 ~

@@ 6

@@ 8

^^ The length of latus rectum of the parabola  $y^2 - 6y - 2x + 5 = 0$  is

@@ 3

@@ 2 ~

@@ 1

@@ 4

^^ The length of latus rectum of the parabola  $x^2 + 8x - 3y + 7 = 0$  is

@@ 1

@@ 2

@@ 3 ~

@@ 4

^^ The length of latus rectum of the parabola  $y^2 + 14y + 4x + 5 = 0$  is

@@ 3

@@ 4 ~

@@ 2

@@ 1

## SECTION 16

^^ If  $x^2 = 2y$  is a parabolic equation, then its directrix is

@@  $y = -\frac{1}{2}$  ~

@@  $x = \frac{3}{2}$

@@  $x = \frac{1}{2}$

@@  $y = \frac{1}{2}$

^^ The equation of a normal to the parabola  $y^2 = 4ax$  at  $(1, 0)$  is given as

@@  $y = 0$  ~

@@  $x = 0$

@@  $-2y = a$

@@  $2x = -a$

^^ The equation of tangent to the parabola  $x^2 = 4ay$  at the point  $(2a, -1)$  is

@@  $y = -x - 2a$

@@  $y = x + 2a$

@@  $y = x + (2a - 1)$

@@  $y = x - (2a + 1)$  ~

^^ The equation of tangent to the parabola  $y^2 = 4ax$  at the point  $(at^2, 2at)$  is

@@  $t^2 y = xt + at$

@@  $ty = x + at^2$  ~

@@  $y = xt + at^2$

@@  $2y = 2xt + at^2$

^^ The vertex of the parabola  $9(x+5)^2 - 3y + 2 = 0$  is

@@  $\left(-5, \frac{2}{3}\right) \sim$

@@  $\left(5, \frac{4}{3}\right)$

@@  $(-1, 2)$

@@  $(0, -2)$

^^ The straight line  $x = 4$  intercept the parabola  $y^2 = 4(x+1)$  at

@@  $(3, \sqrt{20})$  and  $(3 - \sqrt{20}) \sim$

@@  $(3, 4)$  and  $(3 - 4)$

@@  $(3, \sqrt{7})$  and  $(3 - \sqrt{7})$

@@  $(3, \sqrt{5})$  and  $(3 - \sqrt{5})$

^^ The equation of the tangent to the parabola  $x^2 = -2y$  at the point  $(-1, -1)$  is

@@  $y = x + 1$

@@  $y = x - 1$

@@  $y = x \sim$

@@  $y = x + 3$

^^ The directrix axis of the parabola  $x^2 = 4ay$  is

@@  $y = a \sim$

@@  $y = -a$

@@  $x = -a$

@@  $x = a$

^^ Find the equation of the normal to the parabola  $x^2 - 6x - 8y + 1 = 0$  at the point

$\left(1, -\frac{1}{2}\right)$

@@  $2y - 4x + 5 = 0 \sim$

@@  $y - x + 5 = 0$

@@  $y + x - 5 = 0$

@@  $2y - x + 5 = 0$

^^ Find the equation of the normal to the parabola  $x^2 - 2x - y + 6 = 0$  at the point

$(-2, -2)$

@@  $y - 6x - 7 = 0$

@@  $6y - x + 10 = 0 \sim$

@@  $6y + x - 7 = 0$

@@  $y + 6x + 10 = 0$

^^ Find the equation of the normal to the parabola  $y^2 - 7y - 7x + 3 = 0$  at the point  $(-2, -2)$

@@  $y + 11x = 8$

@@  $7y + 11x + 8 = 0$

@@  $7y - 11x - 8 = 0 \sim$

@@  $y - 11x + 8 = 0$

^^ Find the equation of the normal to the parabola  $y^2 - 6y - 2x + 5 = 0$  at the point  $(-2, -2)$

@@  $5y - x + 8 = 0$

@@  $5y + x - 8 = 0$

@@  $y + 5x + 8 = 0$

@@  $y - 5x - 8 = 0 \sim$

^^ Find the equation of the normal to the parabola  $x^2 + 8x - 3y + 7 = 0$  at the point  $(-2, -2)$

@@  $4y - 3x + 2 = 0 \sim$

@@  $y - 3x + 2 = 0$

@@  $4y - x - 2 = 0$

@@  $y + 3x - 2 = 0$

^^ Find the equation of the tangent to the parabola  $x^2 - 6x - 8y + 1 = 0$  at the point  $\left(2, -\frac{1}{2}\right)$

@@  $4y + x = 0 \sim$

@@  $y + 4x = 0$

@@  $y + x + 4 = 0$

@@  $y - 4x = 3$

^^ Find the equation of the tangent to the parabola  $y^2 - 6y - 2x + 5 = 0$  at the point  $(-1, -1)$

@@  $y - 4x - 3 = 0$

@@  $4y + x + 3 = 0 \sim$

@@  $y + 2x + 3 = 0$

@@  $y + 3x + 7 = 0$

^^ Find the equation of the tangent to the parabola  $x^2 + 8x - 3y + 7 = 0$  at the point  $(-1, -1)$

@@  $y + 3x + 4 = 0$

@@  $2y + 2x - 1 = 0$

@@  $y - 2x - 1 = 0 \sim$

@@  $2y - x + 1 = 0$

^^ Find the equation of the tangent to the parabola  $y^2 + 14y + 4x + 5 = 0$  at the point  $(-1, -1)$

@@  $y - 3x + 2 = 0$

@@  $y + 3x - 2 = 0$

@@  $3y + x - 2 = 0$

@@  $3y - x + 2 = 0 \sim$

^^ Find the equation of the tangent to the parabola  $x^2 - 2x - y + 6 = 0$  at the point  $(-1, -1)$

@@  $y - 4x - 3 = 0 \sim$

@@  $y + 4x - 3 = 0$

@@  $4y + x - 3 = 0$

@@  $4y - x + 3 = 0$

^^ The vertex of the parabola  $x^2 - 2x + 4y - 7 = 0$  is

@@  $(1, 2) \sim$

@@  $(2, 1)$

@@  $(-1, -2)$

@@  $(-2, -1)$

^^ The vertex of the parabola  $3x^2 - 5x + 2y - 4 = 0$  is

@@  $\left(\frac{5}{6}, \frac{73}{24}\right) \sim$

@@  $\left(\frac{7}{24}, \frac{5}{6}\right)$

@@  $\left(-\frac{5}{6}, -\frac{73}{24}\right)$

@@  $\left(-\frac{7}{24}, -\frac{5}{6}\right)$

^^ The vertex of the parabola  $y^2 - 6x + 4y + 16 = 0$  is

@@  $(-2, -2)$

@@  $(-2, 2)$

@@  $(2, -2) \sim$

@@  $(2, 2)$

^^ The vertex of the parabola  $(y-2)^2 = -10(x+3)$  is

@@  $(3, 2)$

@@  $(-3, -2)$

@@  $(3, -2)$

@@  $(-3, 2) \sim$

^^ The vertex of the parabola  $(x-2)^2 = -10(y+3)$  is

@@  $(-3, 2) \sim$

@@  $(-2, 3)$

@@  $(-2, -3)$

@@  $(2, 3)$

## SECTION 17

^^ If  $y^2 = 12x$ , find its equation of the tangent at the point whose coordinate is 6

@@  $y - x - 3 = 0 \sim$

@@  $y^2 - x + 6 = 0$

@@  $y + x - 3 = 0$

@@  $y + x + 6 = 0$

^^ Find the equation of the curve with vertex at the origin and directrix is  $x = 6$

@@  $y^2 = -24x \sim$

@@  $y^2 = 12x$

@@  $x^2 = -24y$

@@  $y^2 = 24x$

^^ The equation of tangent to the curve  $x^2 = 4y$  at the point  $(2, 1)$  is

@@  $y + x = 1$

@@  $y - x = -3$

@@  $y - x = -1$  ~

@@  $x - y = -3$

^^ The directrix of  $6y^2 - 9 = 0$  is

@@  $-\frac{3}{8}$  ~

@@  $8$

@@  $-\frac{8}{3}$

@@  $\frac{8}{3}$

^^ The slope of normal to the curve  $x^2 = 4ay$  at  $(at^2, 2at)$  is

@@  $\frac{t^2}{3}$

@@  $-t^2$

@@  $\frac{2t^2}{a}$

@@  $-\frac{2}{t^2}$  ~

^^ The vertex of the curve described by the equation  $x = 3t + 1$  and  $y = 4t^2$  is

@@  $(-1, 0)$

@@  $(1, 0)$  ~

@@  $(0, -1)$

@@  $(0, 1)$

^^ Given that  $x = 2t - 1$  and  $y = t^2 + 2$ , then the equation of the conic is

@@  $(y + 1)^2 = -4(x + 2)$

@@  $y^2 = -4(x - 1)$

@@  $(y - 2)^2 = -4(x + 1)$

$$@@ (x+1)^2 = 4(y-2) \sim$$

^^ The equation of tangent to the curve  $x^2 = -4y$  at the point  $(2, 1)$  is

$$@@ y + x = 3 \sim$$

$$@@ y - x = 3$$

$$@@ y - x + 3 = 0$$

$$@@ 2y + x = 3$$

^^ The equation of tangent to the curve  $y^2 = 4x$  at the point  $(2, 1)$  is

$$@@ y + 2x = 3$$

$$@@ y - 2x = -3 \sim$$

$$@@ y - 2x = 3$$

$$@@ y + x = 2$$

^^ The equation of tangent to the curve  $y^2 = -4x$  at the point  $(2, 1)$  is

$$@@ y + 5x = 2$$

$$@@ y - 2x + 5 = 0$$

$$@@ y + 2x = 5 \sim$$

$$@@ y + x = 5$$

^^ The equation of tangent to the curve  $x^2 = -4y$  at the point  $(-2, -2)$  is

$$@@ y - x = 0 \sim$$

$$@@ y + x = 0$$

$$@@ y - 2x = 5$$

$$@@ y - x = 2$$

^^ The equation of tangent to the curve  $y^2 = 4x$  at the point  $(-2, -2)$  is

$$@@ y + x = -4 \sim$$

$$@@ y - x = 4$$

$$@@ y + 2x = 3$$

$$@@ y - 2x = 4$$

^^ Given that  $x = t^2 + 4$  and  $y = 2t + 4$ , then the equation of conic is

$$@@ (y+4)^2 = 4(x-4)$$

$$@@ (y-4)^2 = 4(x-4) \sim$$

$$@@ (y+4)^2 = 2(x-4)$$

$$@@ (y-4)^2 = -2(x-4)$$

^^ Given that  $x = 2t^2 + 1$  and  $y = t$ , then the equation of conic is

@@  $x^2 = 4(y+1)$

@@  $y^2 = \frac{1}{2}(x-1) \sim$

@@  $x^2 = \frac{1}{2}(y-1)$

@@  $y^2 = 4(x+1)$

^^ Given that  $x = 3 - t^2$  and  $y = 2t$ , then the equation of conic is

@@  $y^2 = 4(x+3)$

@@  $x^2 = 4(y+3)$

@@  $x^2 = -4(y-3)$

@@  $y^2 = -4(x-3) \sim$

^^ Given that  $x = 2t + 3$  and  $y = t^2 - 4$ , then the equation of conic is

@@  $(x+3)^2 = -4(y+4)$

@@  $(x-3)^2 = 4(y+4) \sim$

@@  $(y-3)^2 = -4(x+4)$

@@  $(x+3)^2 = -4(y+4)$

^^ Given that  $x = t^2 - 7$  and  $y = 3t + 7$ , then the equation of conic is

@@  $(y-7)^2 = 9(x+7) \sim$

@@  $(x+7)^2 = 9(y-7)$

@@  $(y+7)^2 = 9(x-7)$

@@  $(x-7)^2 = 9(y+7)$